

Solution #1

$$\begin{aligned} E_f &= \int_{-\infty}^{\infty} x^2(t) dt \\ &= \int_0^{\infty} (Ae^{-\alpha t} + Be^{-\beta t})^2 dt \\ &= \int_0^{\infty} (A^2 e^{-2\alpha t} + B^2 e^{-2\beta t} + 2AB e^{-(\alpha+\beta)t}) dt \\ &= \frac{A^2}{-2\alpha} \left[e^{-2\alpha t} \right]_0^{\infty} + \frac{B^2}{-2\beta} \left[e^{-2\beta t} \right]_0^{\infty} + \frac{2AB}{-(\alpha+\beta)} \left[e^{-(\alpha+\beta)t} \right]_0^{\infty} \\ &= \frac{A^2}{2\alpha} + \frac{B^2}{2\beta} + \frac{2AB}{(\alpha+\beta)} \end{aligned}$$

Solution #2

: There is no such thing as a periodic energy signal. We then more or less easily find:

$e^{-\alpha t} u(t), \alpha > 0 \rightarrow$ non periodic energy signal

$\sin(t) + \cos(3t) \rightarrow$ periodic power signal

$(1 + \text{sinc}(t/2)) \cos(3t) \rightarrow$ non-periodic power signal
(only possibility cuz the other ones are all taken).

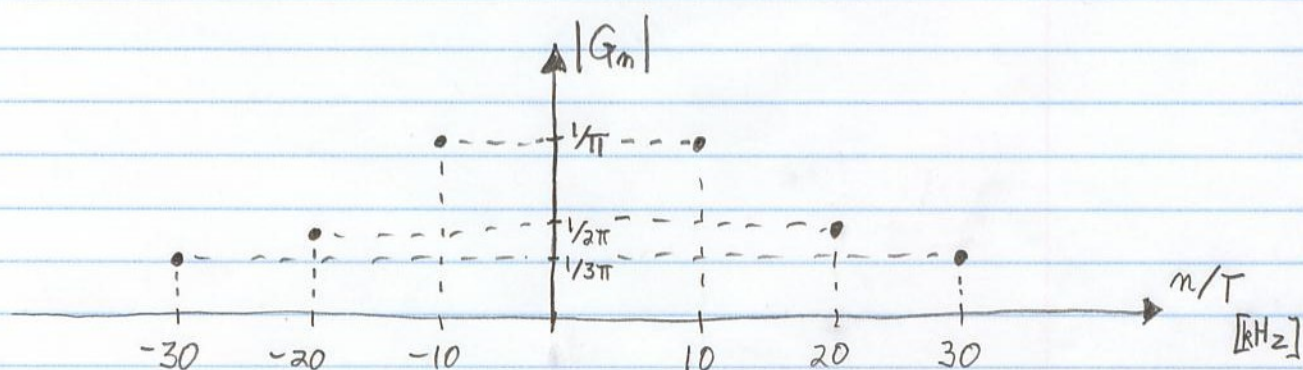
Solution #3(a) Since the signal is real we have $G_{-m} = G_m^*$ and since we are only required to sketch the amplitude spectrum we only need to calculate

$$|G_0| = 1$$

$$|G_{+1}| = |G_{-1}| = 1/\pi \approx 0.3183 \dots$$

$$|G_{+2}| = |G_{-2}| = 1/2\pi \approx 0.15915 \dots$$

$$|G_{+3}| = |G_{-3}| = 1/3\pi \approx 0.1061 \dots$$



Solution #3(b)

$$A_0 = G_0 = A/2$$

$$A_m = 2 \operatorname{Re}(G_m) = 0 \quad \text{si } m = 1, 2, 3, \dots$$

$$B_m = -2 \operatorname{Im}(G_m) = \frac{-A}{\pi m} \quad \text{si } m = 1, 2, 3, \dots$$

$$\begin{aligned} g(t) &= \frac{A}{2} - \sum_{n=1}^{\infty} \frac{A}{\pi n} \sin(2\pi n t / T) \\ &= A \left(\frac{1}{2} - \frac{1}{\pi} \left(\sum_{n=1}^{\infty} \frac{1}{n} \sin(2\pi n t / T) \right) \right) \end{aligned}$$

works; verified with Sage Math.