## Answers to EEE210 final exam AY2016-2017

1. (a) i. Replace Zener diode by its model. Then show

 $V_{in} < 0 \Leftrightarrow \text{Zener forward biased}$   $0 < V_{in} < 9 \text{ V} \Leftrightarrow \text{Zener reverse biased off}$  $9 \text{ V} < V_{in} \Leftrightarrow \text{Zener reverse conduction}$ 

The given  $V_{out}$  vs  $V_{in}$  is easily obtained.

ii. Zener diode is initially in reverse conduction. Then:

$$V_C(t) = 6 + 6 e^{-t/(2 \text{ ms})} \text{ V}$$

The state of the diode changes at 1.386 ms.

(b) Depending on how you solve the problem you obtain

$$1810~\Omega < R < 1995~\Omega$$

and

$$3.35 \times 10^{-15} \text{ A} < I_S < 3.78 \times 10^{-15} \text{ A},$$

again, depending on how you solve.

2. (a)

$$I_D = 2.646 \text{ mA}$$

$$V_{GS} = 2.23 \text{ V}$$

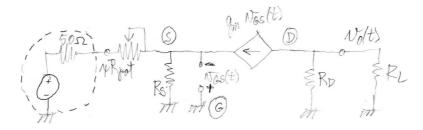
$$V_{DS} = 12.62 \text{ V}$$

(b)

$$R_E = 5.047619 \text{ k}\Omega$$

$$R_C = 4.5 \text{ k}\Omega$$

3. (a) The AC model is:

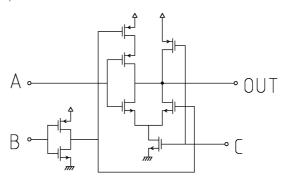


Use circuit analysis to obtain the voltage gain.

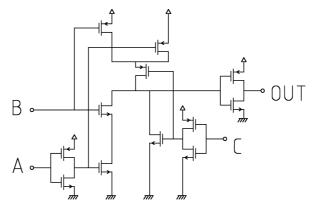
(b) Obvious from the above and  $R_{\text{var}} = x R_{\text{pot}}$ .

- (c)  $V_{GSQ} = 2.4286 \text{ V}, I_{DQ} = 12.8571 \text{ mA}.$
- (d)  $R_S = 330 \ \Omega$ .
- (e)  $R_D = 1 \text{ k}\Omega$ .
- (f)  $V_{DSQ} = 7.89286 \text{ V}, V_{GQ} = 6.67857 \text{ V}.$
- (g)  $R_1 = 330 \text{ k}\Omega, R_2 = 120 \text{ k}\Omega.$
- (h) Obvious from the above and  $R_{\text{var}} = x R_{\text{pot}}$ .
- (i)  $R_{\rm pot} = 100 \ \Omega$ .
- (j)  $Z_{in} = (100 x + 15.865) \Omega$ .
- (k)  $Z_{out} = 1 \text{ k}\Omega, \forall x.$

4. (a)  $\overline{A} \wedge B \vee \overline{C} = \overline{(A \vee \overline{B}) \wedge C}$  which leads to the circuit (requires 8 MOSFETs):



Alternatively, one can design the circuit for  $\overline{\overline{A} \wedge B \vee \overline{C}}$  and finish with an inverter as in the following (requires 12 MOSFETs):



- (b) i.  $v_{out} = -6.2 + 22.4 v_{in} 11.2 v_{in}^2$ 
  - ii. 1 V  $\leq v_{in} \leq 1.625 \text{ V}$
  - iii. Graphically we find values close to the ones below.
  - iv.  $V_{iH}=1.726874~{
    m V},~V_{oL}=0.38575827~{
    m V},~V_{iL}=1.0446429~{
    m V},~V_{oH}=4.9776786~{
    m V}.$  It follows that

$$NM_H = 3.2508046 \text{ V}$$

$$NM_L = 0.65888463~{\rm V}$$

$$NM = \frac{NM_H + NM_L}{2} = 1.954844615 \text{ V}$$